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**B.TECH**  
**(SEM I) THEORY EXAMINATION 2020-21**  
**ENGINEERING MATHEMATICS-I**

Time: 3 Hours

Total Marks: 100

Note: 1. Attempt all Sections. If require any missing data; then choose suitably.

## SECTION A

1. Attempt all questions in brief.

2 x 10 = 20

Qno.	Question	Marks	CO
a.	Prove that the matrix $\frac{1}{\sqrt{2}} \begin{bmatrix} 1 & 1 \\ i & 1 \end{bmatrix}$ is unitary.	2	1
b.	State Rank-Nullity Theorem.	2	1
c.	State Rolle's Theorem.	2	2
d.	Discuss all the symmetry of the curve $xy = x + a$	2	2
e.	If $u = f(y, z), z = x, x = y$ , prove that $\frac{\partial u}{\partial x} + \frac{\partial u}{\partial y} + \frac{\partial u}{\partial z} = 0$	2	3
f.	If $x = e \sec u, y = e \tan u$ , then evaluate $\frac{dy}{dx}$ .	2	3
g.	Evaluate $\int e^y dy dx$ .	2	4
h.	Calculate the volume of the solid bounded by the surface $x = 0, y = 0, x + y + z = 1$ and $z = 0$ .	2	4
i.	Show that the vector $\vec{V} = x^2 y \hat{i} + y^2 z \hat{j} + x^2 z \hat{k}$ is solenoidal.	2	5
j.	State Green's theorem.	2	5

## SECTION B

2. Attempt any three of the following:

Qno.	Question	Marks	CO
a.	Find the inverse of the matrix $A = \begin{bmatrix} 2 & 3 & 4 \\ 4 & 3 & 1 \\ 1 & 2 & 4 \end{bmatrix}$	10	1
b.	If $y = e^x$ , prove that $(1 + x^2)y_{n+2} + [(2n+2)x - 1]y_{n+1} + n(n+1)y_n = 0$ .	10	2
c.	If $u = v + w + x + y + z$ , $\frac{\partial u}{\partial x} = \frac{\partial v}{\partial x} + \frac{\partial w}{\partial x} + \frac{\partial x}{\partial x} + \frac{\partial y}{\partial x} + \frac{\partial z}{\partial x}$ , $\frac{\partial u}{\partial y} = \frac{\partial v}{\partial y} + \frac{\partial w}{\partial y} + \frac{\partial x}{\partial y} + \frac{\partial y}{\partial y} + \frac{\partial z}{\partial y}$ , $\frac{\partial u}{\partial z} = \frac{\partial v}{\partial z} + \frac{\partial w}{\partial z} + \frac{\partial x}{\partial z} + \frac{\partial y}{\partial z} + \frac{\partial z}{\partial z}$ , Show that: $\frac{\partial u}{\partial x} + \frac{\partial u}{\partial y} + \frac{\partial u}{\partial z} = \frac{1}{2} + \frac{4xy}{3u} + \frac{xy}{v} + \frac{yz}{w} + \frac{zx}{27uvw} + \frac{16xyz}{27uvw}$	10	3
d.	Evaluate by changing the variables $\iint_R xy \, dx \, dy$ where R is the region bounded by the parallelogram $x + y = 0, x + y = 2, 3x - 2y = 0$ and $3x - 2y = 3$ .	10	4
e.	Use divergence theorem to evaluate the surface integral $\iint_S x \, dy \, dz + y \, dz \, dx + z \, dx \, dy$ where S is the portion of the plane $x + 2y + 3z = 6$ which lies in the first octant.	10	5



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## SECTION C

3. Attempt any *one* part of the following:

Qno.	Question	Marks	CO
a.	Find non-singular matrices P and Q such that PAQ is normal form. $\begin{matrix} 1 & 1 & 2 \\ 1 & 2 & 3 \\ 0 & 1 & 1 \end{matrix}$	10	1
b.	Find the eigen values and the corresponding eigen vectors of the following matrix. $A = \begin{pmatrix} 2 & 0 & 1 \\ 0 & 3 & 0 \\ 1 & 0 & 2 \end{pmatrix}$	10	1

4. Attempt any *one* part of the following:

Qno.	Question	Marks	CO
a.	Find the envelope of the family of lines $ax + by = 1$ , where $a$ and $b$ are connected by the relation $a^2 + b^2 = c^2$	10	2
b.	If $y = \sin(m \sin^{-1}x)$ , find the value of $y_n$ at $x=0$ .	10	2

5. Attempt any *one* part of the following:

Qno.	Question	Marks	CO
a.	Divide 24 into three parts such that continued product of first, square of second and cube of third is a maximum.	10	3
b.	If $u \sec^{-1} \frac{x}{a} = v \sec^{-1} \frac{y}{b}$ , prove that $x^2 - y^2 = 2 \cot u$ . Also evaluate $x^2 - y^2$ .	10	3

6. Attempt any *one* part of the following:

Qno.	Question	Marks	CO
a.	Evaluate the following integral by changing the order of integration $\int_0^1 \int_0^{1-x} dy dx$ .	10	4
b.	A triangular thin plate with vertices (0,0), (2,0) and (2,4) has density $\rho = 1 - x - y$ . Then find: (i) The mass of the plate. (ii) The position of its centre of gravity G.	10	4

7. Attempt any *one* part of the following:

Qno.	Question	Marks	CO
a.	A fluid motion is given by $\vec{v} = y \sin z \hat{i} + x \sin z \hat{j} + xyz \cos z \hat{k}$ . Is the motion irrotational? If so, find the velocity potential.	10	5
b.	Verify Stoke's theorem for the function $\vec{F} = x \hat{i} + xy \hat{j}$ integrated round the square whose sides are $x=0, y=0, x=a, y=a$ in the plane $z=0$ .	10	5